



LOYOLA COLLEGE (AUTONOMOUS), CHENNAI – 600 034

B.Sc. DEGREE EXAMINATION - MATHEMATICS

THIRD SEMESTER – NOVEMBER 2015

MT 3504 - INTEGRAL TRANSFORMS & PARTIAL DIFF. EQUATIONS

Date : 06/11/2015
Time : 09:00-12:00

Dept. No.

Max. : 100 Marks

PART – A

Answer ALL the questions:

(10 x 2 = 20 marks)

1. Form the partial differential equations by eliminating a and b from $z = ax + by + a^2 + b$.
2. Find the complete solution of $p+q=pq$.
3. Find $L\left(\frac{e^{at} - 1}{a}\right)$.
4. Find $L(t^3 e^{-3t})$.
5. Find $L^{-1}\left(\frac{s-2}{(s-2)^2 + 5^2}\right)$.
6. Find $L^{-1}\left(\frac{3s+1}{(s+1)^4}\right)$.
7. If $f_c(s)$ is the Fourier Cosine transform of $F(x)$, then show that Fourier Cosine transform of $F\left(\frac{x}{a}\right)$ is $af_c(as)$.
8. State convolution theorem on Fourier transforms.
9. Find Fourier sine transform of $f(x) = \frac{1}{x}$.
10. State parseval's identity for Fourier series.

PART – B

Answer any FIVE questions:

(5 x 8 = 40 marks)

11. Solve: $z^2 = xypq$.
12. Solve: $q = -px + p^2$.
13. Find $L\{F(t)\}$, if
$$F(t) = \begin{cases} (t-1)^2, & t > 1 \\ 0, & 0 < t < 1 \end{cases}$$
14. Show that $\int_0^{\infty} t e^{-3t} \sin t \, dt = \frac{3}{50}$.
15. If $L^{-1}\left\{\frac{s^2-1}{(s^2+1)^2}\right\} = t \cos t$, then find $L^{-1}\left\{\frac{9s^2-1}{(9s^2+1)^2}\right\}$.
16. Find $L^{-1}\left\{\frac{3p+7}{p^2-2p-3}\right\}$.

17. If $f(s)$ is the Fourier transform of $F(x)$, then prove that $\frac{1}{a} f\left(\frac{s}{a}\right)$ is the Fourier transform of $F(ax)$.

18. Show that the Fourier transform of $f(x) = e^{-\frac{x^2}{2}}$ is $\sqrt{2\pi} e^{-\frac{p^2}{2}}$.

PART – C

Answer any TWO questions:

(2 x 20 = 40 marks)

19. (a) Solve $z^2(p^2x^2 + q^2) = 1$.

(b) Solve $(1+y)p + (1+x)q = z$. (10 +10)

20. Using Laplace transform solve the equation $(D^2 - 3D + 2)y = 1 - e^{2t}$, $y = 1$, $D_y = 0$, when $t = 0$.

21. a) Find $L^{-1}\left\{\frac{1}{s} \log \frac{s+2}{s+1}\right\}$.

b) Solve: $\int_0^{\infty} f(x) \cos x dx = e^{-1}$. (10 +10)

22. Find the sine transform of $\frac{x}{1+x^2}$.

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